

UNIT 3 LESSON 1 – MIDPOINT AND ENDPOINT

Line segment is a part of the line that has two endpoints

$$(x_1, y_1) \quad \text{AND} \quad (x_2, y_2)$$

The length of a line segment can be found using the distance formula.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

The midpoint is the point on the line segment that divides it into two equal parts.

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Midpoint formula:

Example 1) Calculate the midpoint of the line segment with endpoints (-2, 1) and (4, 10).

Step 1: Substitute endpoints into formula

$$\text{Midpoint formula } \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = \left(\frac{-2+4}{2}, \frac{1+10}{2} \right)$$

Step 2: Calculate the midpoint

$$\left(\frac{-2+4}{2}, \frac{1+10}{2} \right) = \left(\frac{2}{2}, \frac{11}{2} \right) = \left(1, \frac{11}{2} \right)$$

Example 2) A line segment has one endpoint at (12, 0) and a midpoint of (10, -2). Locate the second endpoint.

Step 1: Substitute endpoints into formula

$$\text{Midpoint} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = (10, -2) = \left(\frac{12+x_2}{2}, \frac{0+y_2}{2} \right)$$

Step 2: Find the value of x

$$\begin{aligned} 10 &= \frac{12 + x_2}{2} \\ 2 * 10 &= \frac{12 + x_2}{2} * 2 \\ 20 &= 12 + x_2 \\ x_2 &= 8 \end{aligned}$$

Step 3: Find the value of y

$$\begin{aligned} -2 &= \frac{0 + y_2}{2} \\ 2 * -2 &= \frac{0 + y_2}{2} * 2 \\ -4 &= 0 + y_2 \\ y_2 &= -4 \end{aligned}$$

YOU TRY!!!

EX 3) Find the midpoint of the coordinates (22, -9) and (-8, 25)

EX 4) Find the 2nd endpoint given the endpoint (1, 5) and the midpoint (2.5, 7.5)